

# Analysis of Low-Oversampled Staggered SAR Data

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**Abstract**—The combination of SCan-On-REceive with continuous variation of the pulse repetition interval during transmission (staggered operation) is a viable option for the acquisition of high-resolution synthetic aperture radar (SAR) data over wide areas. Since the acquired data are not uniformly sampled and contain gaps within the synthetic aperture mainly due to the interruption of reception during transmission (i.e., due to blockage), proper reconstruction strategies must be considered in order to minimize artifacts. Conventionally, large oversampling rates are required to ensure low ambiguity levels, but this is not always feasible due to data-rate constraints. This article presents a detailed analysis of the blockage recovery in the low-oversampling case. Moreover, we propose a data adaptive strategy to optimally perform this step, ensuring the best performance for point-like targets and avoiding degradation for distributed scatters. This paper also presents simulation results that show the impact of staggered data for interferometric applications.

**Index Terms**—Blockage, low-oversampling, staggered SAR, spectral estimation.

## I. INTRODUCTION

IN THE past decade, increasing focus has been given to the development of new synthetic aperture radar (SAR) concepts capable of delivering both high resolution and wide coverage [1]–[5]. In order to overcome the fundamental limitation imposed by the direct relation between swath width and azimuth resolution, the solutions usually consider multiple elevation beams in combination with SCan-On-REceive (SCORE) or the acquisition by multiple subapertures in the along-track direction [2], [4], [6]–[11].

The authors in [5] demonstrated the staggered SAR concept, which together with SCORE allows for the coverage of a continuous wide swath with high resolution. To achieve that, the pulse repetition interval (PRI) is continuously varied during the acquisition causing the blockage—i.e., the instants during

transmission when the radar cannot receive the backscattered echoes—to move along the swath.

Several schemes can be used to control the variation of the PRI, e.g., pseudorandom variation, slow linear variation or fast linear variation. In [5], it was shown that optimum performance in terms of azimuth-ambiguity-to-signal-ratio (AASR) is achieved by combining a few fast linearly varying PRI sequences (e.g., 7). Such scheme is usually able to distribute the blockage along the swath in a way that no consecutive samples are missed in azimuth. If enough oversampling is available, the missing data can be interpolated and a performance similar to the constant pulse repetition frequency (PRF) case can be achieved. Moreover, in this case, the staggered operation has the further advantage of leading to smeared azimuth ambiguities.

Given the periodicity of the nonuniform pattern, an alternative for the processing of the staggered data is the use multichannel reconstruction approaches [1], [12]. However, such methods are impacted by noise scaling and by the back-folding of the nonlimited spectrum, especially for long PRI sequences [13]. In order to efficiently perform the SAR focusing, the staggered data can be interpolated to a uniform grid allowing for the use of conventional frequency-domain SAR processing techniques. This resampling can be performed, e.g., with the best linear unbiased estimator (BLU), as suggested in [5], or with a nonuniform cardinal sine (sinc) kernel, as described in [14]. Alternatively, the data can be focused directly from the nonuniform grid, e.g., considering the nonuniform discrete Fourier transform [15], or employing time domain back-projection. In all cases, the presence of the blockage potentially degrades the quality of the focused data, especially if acquiring with a low average oversampling ratio.

Staggered SAR is currently the baseline acquisition mode of the Tandem-L concept [16]. Tandem-L's goal is to acquire single/dual-polarimetric data over a 350 km ground-swath and fully polarimetric data over a 175 km ground-swath, with an azimuth resolution of around 7.5 m. Optimum oversampling factors are calculated considering the ambiguity level requirements and the designed PRI sequence, and amount to 2.3 and 1.9 for the dual-pol and quad-pol modes. Although an experimental quad-pol mode with 350 km swath is desirable, due to range ambiguity constraints its mean PRF on transmit has to be limited to 1200 Hz per channel. This corresponds to an oversampling ratio of only 1.1, in which case the standard processing solution based on BLU resampling suggested in [5] cannot be used.

Another mission which can benefit from the staggered operation mode is the NASA-ISRO SAR (NISAR) mission [17].

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TABLE I  
PARAMETERS OF TANDEM-L AND NISAR EXPERIMENTAL SCENARIOS

	<b>Tandem-L</b>	<b>NISAR</b>
Polarization	Quad-pol	Single-pol
Swath width	350 km	240 km
Reflector diameter	15 m	12 m
3dB Doppler bandwidth	1200 Hz	1536 Hz
Chirp bandwidth	80 MHz	40 MHz
Chirp duration	33 $\mu$ s	47 $\mu$ s
Mean PRF on Tx	1200 Hz	1650 (2000) Hz
Processed bandwidth	1100 Hz	1100 Hz
Antenna correlation length	833 $\mu$ s	636 $\mu$ s
PRI sequence	More elaborated with 7 sub-sequences [5]	
Min PRI	664 $\mu$ s	496 (386) $\mu$ s
Mean PRI	833 $\mu$ s	606 (500) $\mu$ s
Max PRI	992 $\mu$ s	710 (604) $\mu$ s

NISAR aims to acquire data over a 240 km wide swath with 6 m azimuth resolution. As described in [18], if employing a constant PRF for transmission, the gaps amount to 10% of the dual-pol swath (ascending-only or descending-only) and can be mitigated if a coarser range resolution is acceptable. If continuous swath coverage in each individual pass is required, the staggered mode can be used [19]. In order to fulfill the ambiguity requirements, the staggered operation would require a mean PRF on transmit of around 2400 Hz, which is much higher than the current maximum value of 1650 Hz imposed by limited downlink capacity. Nevertheless, for some applications the degradation of the ambiguity level caused by acquiring with a reduced PRF may be acceptable.

Both aforementioned staggered NISAR and experimental Tandem-L modes employ low average oversampling ratios (see parameters summary in Table I). Hence, in both cases the focused SAR image might contain nonnegligible artifacts, specially for areas presenting high contrast and containing strong point-like targets. A first solution for the imaging of low-oversampled staggered data was proposed in [20]. The method consists in two steps: first, the recovery of the blockage using an spectral estimator (SE) for nonuniformly sampled data [21], [22]; and second, the resampling of the data to the uniform grid by minimizing the ambiguity energy in a multichannel reconstruction scheme [23]. While the approach is able to considerably reduce the artifacts of strong targets, it is suboptimal in the sense that it does not consider the target characteristics during the data recovery.

In [24], we first suggested a few modifications to the approach in [20], which intended to improve the reconstruction of point-like targets while avoiding the degradation of distributed scatterers (DSs). In this article, the suggested approach for the processing of low-oversampled staggered data is discussed in depth, with the aid of an extensive analysis of the blockage recovery in Section II. Section III includes a detailed description of the complete approach, including the outline of optional steps and a discussion of when they should be used. Finally, in Section IV, we validate the proposed methodology with simulated staggered SAR data and provide first examples of the impact of the staggered operation for interferometric applications. Conclusion is drawn in Section V.

## II. BLOCKAGE RECOVERY

Standard PRI design for staggered SAR acquisitions ensures that consecutive azimuth samples are not lost in either the raw or range-compressed data domains, depending on the adopted processing approach [25]. However, even when employing such optimum design strategy, if the mean effective PRF on transmit is close to the Doppler bandwidth, the signal can be locally under-sampled. In this case, the blockage will introduce large gaps in the signal (in terms of the signal bandwidth), and the recovery of this missing data becomes a major challenge to the handling of the staggered data.

The main contribution of [20] to the processing of low-oversampling SAR data is precisely the dedicated treatment given to the blockage. Instead of directly interpolating the available data into a uniform grid as conventionally done in the high PRF case [25], the authors handle the reconstruction in two steps: first, the missing data of the blockage is recovered still in the nonuniform grid; and second, the full vector is resampled to the uniform grid. Hence, if the recovery of the missing data is successful, the resampling is performed on a properly sampled data vector.

If a time domain back-projection approach is employed for the SAR focusing, the resampling to the uniform grid can be avoided. However, the prior recovery of the blockage may still be required depending on the local sampling characteristics (i.e., its average oversampling and deviation to the uniform grid [26], [27]). In the remaining of this section, we address the significance of this recovery for the resulting azimuth side-lobe level (see Section II-A). Moreover, we show the performance of the iterative adaptive approach for missing data (MIAA) and BLU for the blockage recovery considering different simulation scenarios (in Section II-B).

### A. On the Necessity of the Blockage Interpolation

The necessity of the blockage interpolation can be evaluated by considering a simplified case where samples from a uniformly sampled signal are periodically missed. If the blockage is neither recovered nor accounted for, the back-projection integral for a single scatter can be approximated as

$$\begin{aligned}
 s_B[n] &= \sum_{-LSA/2}^{+LSA/2} (s_{rc}[m] - s_{rc}[m]\Pi[m; T_B]) h_{az}[m - n] \\
 &= s_{NB}[n] - s_{rc}[n]\Pi[n; T_B] * h_{az}[n]
 \end{aligned} \quad (1)$$

where LSA is the size of the synthetic aperture,  $s_{rc}$  is the range-compressed pulse,  $s_B$  is the focused signal,  $s_{NB}$  is the focused signal considering the complete dataset case (i.e., no blockage), and  $h_{az}$  is the azimuth match filter and  $\Pi[\cdot; T_B]$  is an impulse train which assumes one every  $T_B$  samples (i.e., at blockage locations) and zero everywhere else. The range variable has been omitted for simplicity, and we assume that the signal can be interpolated with an arbitrary accuracy in range.

Alternatively, the back-projection integral can be performed over the available samples only, i.e., considering the new

nonuniformly sampled grid described by the time instants

$$t[n] = n\Delta t + g[n] = n\Delta t + \left( \sum_{i=0}^{\lfloor \frac{N-1}{T_B} \rfloor} i\chi_{[iT_B, (i+1)T_B)} \right) [n] \quad (2)$$

where  $g$  gives the deviation of the nonuniform grid from a uniform one with constant sampling equal to  $\Delta t$ , and has a staircase shape for the case of missing samples from a uniform grid. The staircase shape is represented by the summation on the right-hand side of (2), where  $i$  is an integer given by  $\lfloor n/T_B \rfloor$  and  $\chi_A$  is the indicator function of the interval  $A$ . The compressed signal is then approximated by

$$s_{\text{NU}}[n] = \frac{1}{\Delta t} \sum_{-LSA/2}^{+LSA/2} s_{\text{rc},\text{avl}}[m] h_{\text{az},\text{avl}}[m-n] \delta[m] \quad (3)$$

where the subscript  $\text{avl}$  indicates that only the available samples are considered, and  $\delta[\cdot]$  accounts for the variability of the time increments. For example, for the sampling pattern described by (2), the time increments can be approximated as

$$\delta[n] = t[n+1] - t[n] = \Delta t + \Pi[n; T_B - 1]. \quad (4)$$

Notice that (1) can be converted to (3) by considering additional tapering of the samples around the blockage.

If the blockage is interpolated, the focused signal is given by

$$\begin{aligned} s_{\text{I}}[n] &= \sum_{-LSA/2}^{+LSA/2} s_{\text{rc},i}[m] h_{\text{az}}[m-n] \\ &= s_{\text{NB}}[n] + \psi[n] \Pi[n; T_B] * h_{\text{az}}[n] \end{aligned} \quad (5)$$

where  $s_{\text{rc},i}$  is the pulse after blockage interpolation, and  $\psi$  is the interpolation error.

Assuming  $s_{\text{NB}}$  as reference, the error in the focused signals above can be described in the discrete-time-Fourier-transform (DTFT) domain as

$$\sigma_B^2 = \int_{-B_{\text{az}}/2}^{B_{\text{az}}/2} |S_{\text{NB}}(e^{j\Omega}) * \Pi(e^{j\Omega})|^2 |H_{\text{az}}(e^{j\Omega})|^2 d\Omega \quad (6)$$

$$\sigma_{\text{NU}}^2 = \int_{-B_{\text{az}}/2}^{B_{\text{az}}/2} |S_{\text{NB}}(e^{j\Omega}) * \Delta(e^{j\Omega})|^2 |H_{\text{az}}(e^{j\Omega})|^2 d\Omega \quad (7)$$

and

$$\sigma_{\text{I}}^2 = \int_{-B_{\text{az}}/2}^{B_{\text{az}}/2} |\Psi(e^{j\Omega}) * \Pi(e^{j\Omega})|^2 |H_{\text{az}}(e^{j\Omega})|^2 d\Omega \quad (8)$$

respectively, where  $B_{\text{az}}$  is the Doppler bandwidth, the capital letters indicate the DTFT, and the fact that the DTFT of an impulse train is a frequency domain impulse train has been used. Equation (7) can also be used to describe the error in the staggered SAR case, i.e., when the complete input is nonuniform. The error depends on the characteristics of the blockage (and nonuniformity of the grid), on the signal and, eventually, on the interpolator. However, from (6) and (8), we can conclude that

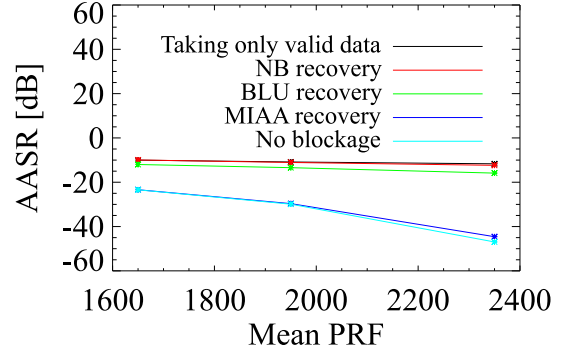


Fig. 1. Mean AASR obtained after back-projecting from the nonuniform grid. Five cases are shown: considering only the valid samples for the back-projection (equivalent to (3), in black), recovering the blockage with a nearest-neighbor interpolator (in red), recovering the blockage with BLU (in green), recovering the blockage with a SE (in blue), and when no blockage is present (in turquoise). The curves show the behavior of the AASR for increasing mean PRF on transmitter.

whenever the spectral power of the interpolation error is small in comparison to the one of the signal, the recovery improves the performance. Conversely, if the recovery fails and the error power is of the order of the signal, then recovery step should not be performed.

Fig. 1 shows simulation results considering an ideal point target and a staggered SAR acquisition with the parameters described in the third column of Table I (staggered NISAR example). The plot shows the mean azimuth-ambiguity-to-signal-ratio (AASR) over the swath obtained after back-projecting from the non-uniform grid. The AASR is computed here as the difference between the staggered SAR integrated-side-lobe-ratio (ISLR) and the ISLR of a constant PRI SAR system with a PRF equal to the mean staggered PRF on transmit, same values for the other system and processing parameters, and an azimuth antenna pattern equal to zero outside the interval  $[-\text{PRF}_{\text{mean}}, \text{PRF}_{\text{mean}}]$  [28]. Five recovery strategies are shown: considering only the valid samples for the back-projection (equivalent to (3), solid black), recovering the blockage with a nearest-neighbor interpolator (solid red), recovering the blockage with BLU (solid green), recovering the blockage with a SE (solid blue), and when no blockage is present (i.e., the reference, solid turquoise). Notice that regardless of the PRF, the spectral estimator (in this case, MIAA [22]) and BLU provide better results than when no recovery is applied. Moreover, MIAA ensures a performance which is very close to the nonblockage case. On the other hand, nearest-neighbor interpolation brings almost no improvement when compared to the case when only the available data are considered, i.e., in this case the spectral power of the error approaches the one of the signal.

The use of back-projection directly from the nonuniform grid (i.e., without resampling) can potentially diminish the propagation of interpolation errors and noise scaling. However, this is not necessarily the case for the modes examined in this article, since the reconstruction of the low-oversampled staggered signal from its nonuniform samples is not ideal [26], [27]. For the simulation shown in Fig. 2 the parameters in the third column of Table I were also considered, and the goal was to compare



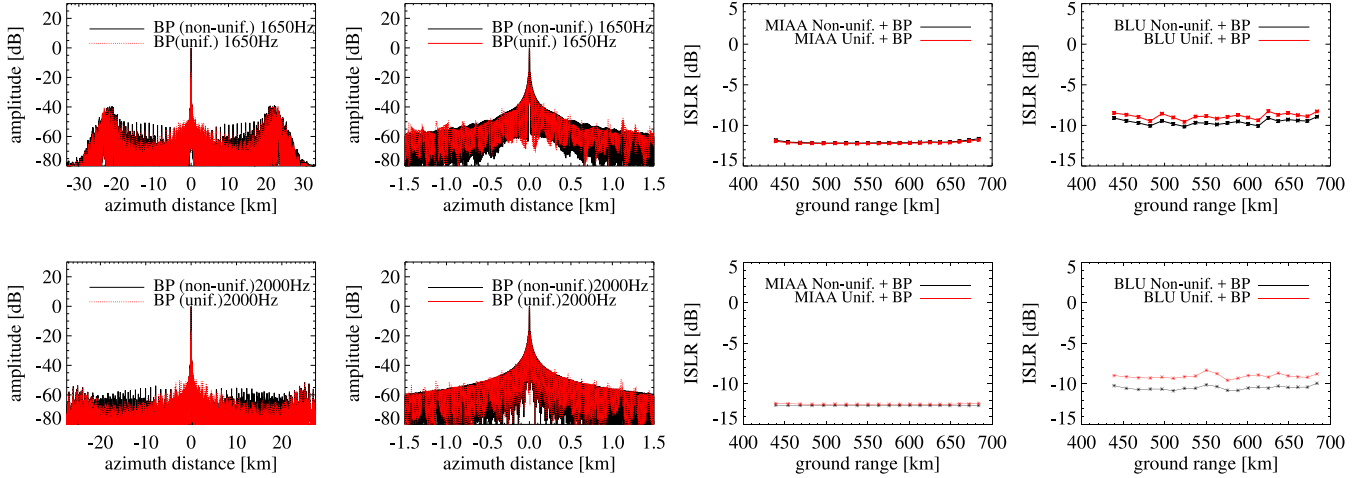


Fig. 2. Plots in the first and second column show zooms of the IRF obtained when recovering with the SE and back-projecting from the nonuniform grid (solid black), and considering an additional resampling step (solid red). The plots in the third and fourth columns show the variation of the ISLR over the swath when using MIAA and BLU, respectively. The top row corresponds to a PRF of 1650 Hz, whereas the bottom one corresponds to a relaxed case with mean PRF of 2000 Hz.

the focusing when back-projecting directly from the nonuniform grid and when performing an additional resampling step before the integration. The plots on the first and second columns show zooms of the impulse response function (IRF) obtained when recovering with the SE and back-projecting from the nonuniform grid (in black), and considering an additional resampling step (in red). The plots in the third and fourth columns show the variation of the AASR over the swath when using MIAA and BLU, respectively. The top row corresponds to a mean PRF on transmit of 1650 Hz, whereas the bottom one corresponds to a relaxed case with a mean PRF of 2000 Hz. Note that in both PRF scenarios, the resampling to the uniform grid leads to artifacts related to the propagation of blockage recovery errors. Those are recognizable as periodic spurious lobes in the second IRF zooms (second column). Moreover, in the results obtained after the resampling, the side-lobe energy concentrates near the main one, while it is spread when back-projecting from the nonuniform grid. The resulting integrated side lobe energy using both processing strategies is similar. In fact, for the 1650 Hz and MIAA recovery case, there is actually a slight degradation of the ISLR when back-projecting from the nonuniform grid due to a small increase of the overall side-lobe energy caused by the nonuniformity (see second column) [26]. The same is not true when recovering the data with BLU, since in this case the recovery errors are considerably larger and their propagation during the resampling dominates.

Finally, we make a note on the discrete implementation of the back-projection integral. The discrete back-projection integral for the complete staggered signal can also be described by (3) and (4). In (4), we considered the left-Riemann approximation (up to a multiplicative constant). However, the discretization (or equivalently, the tapering of the staggered signal), can be done in different ways [29], [30]. The use of a scheme that averages time increments, e.g., the Trapezoidal rule, will potentially decrease artifacts caused by the strong nonuniformity of the elaborated staggered sampling pattern used here. This

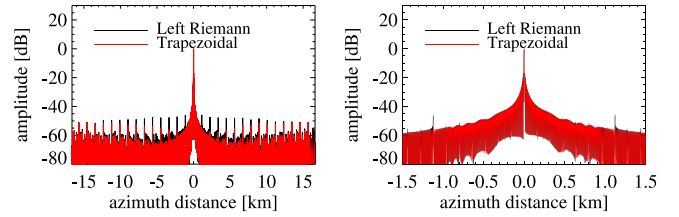


Fig. 3. Zooms of the obtained IRF response using back-projection from the nonuniform grid considering the left-Riemann sum and Trapezoidal rule.

can be observed in the IRF responses shown in Fig. 3, also corresponding to the parameters in third column of Table I. However, here an ideal case with no-blockage was considered to avoid propagation of the recovery errors. Both results were focused by back-projecting the signal from the nonuniform grid. The curves in black consider the left-Riemann sum, while the ones in red correspond to the trapezoidal rule.

### B. Performance of Super-Resolution SEs

The reconstruction of signals from nonuniform samples has been extensively studied by the signal processing community [26], [31]–[33]. For example, Yao and Thomas showed that perfect reconstruction of band-limited signals is possible using Lagrange interpolation functions if the nonuniform sampling instants do not deviate from the uniform grid by more than a quarter of the signal bandwidth [32]. In the case of staggered SAR acquisitions, not only is the spectrum nonlimited, but also the deviation from the uniform grid can be much larger than the 3 dB observation time. For example, for the experimental 350 km swath/quad-pol mode of the Tandem-L concept described in the second column of Table I, the deviation is around 2.6 times larger than the Yao and Thomas condition, whereas for a staggered NISAR acquisition such as the one described in the third column of Table I, it is about 2.7 times (for a segment size

given by the correlation length [5]). Hence, more sophisticated reconstruction approaches are required.

The use of parametric and nonparametric SE for the recovery of interrupted SAR data has been demonstrated in [34], [35]. SEs have been also suggested for the recovery of the blockage in staggered SAR acquisitions in [20]. More specifically, the authors employed the nonuniform iterative adaptive approach for missing data (MIAA) for their recovery step [21], [22].

In the aforementioned studies, the SE are applied to all missing data, i.e., no distinction concerning the characteristics of the imaged target is made. However, such algorithms are derived for line spectra and, hence, are specially suitable for the reconstruction of raw data from point targets. In fact, experiments with TerraSAR-X data in [36] showed that the performance of different SEs is not satisfactory when recovering gapped data from distributed scatters. Note that in that case, the data were missing in a uniform grid due to the synchronization link between the TerraSAR-X and TanDEM-X satellites [37]. In the context of staggered SAR, the performance of the data recovery is further impaired by the strong nonuniformity of the sampling. In fact, the distribution of the nonuniform samples and the choice of the spectral grid used for the reconstruction are known to impact the performance of the spectral estimation [21], [26], [27].

In order to recover the blockage of a staggered SAR dataset in an optimum way, it is necessary to understand the behavior of the recovery methods. This is the main goal of the remaining of this section. For that, we include a brief recap of the super-resolution SE of choice and provide analysis of the performance of the blockage recovery with respect to different aspects (e.g., the type of data being recovered; the available signal-to-clutter ratio (SCR), the sequence design and the chosen spectral grid). All the analysis results presented in the following were obtained through one-dimensional (1-D) simulations considering the experimental quad-pol/ 350 km swath mode of the Tandem-L concept, unless otherwise specified (see second column of Table I).

1) *MIAA for Data Recovery*: Methods for data recovery based on super resolution spectral estimation generally model data segments as composed of available ( $y_g$ ) and missing ( $y_m$ ) contributions [22], [35], [38]. A first estimation of the spectrum is made from the available samples, and the recovery of the missing ones is obtained from this estimate and a certain fitting criteria (e.g., least-squares or maximum-likelihood). An updated estimation of the spectrum is performed using the now complete data segment and the data-recovery/spectrum-estimation procedure is possibly repeated until convergence.

Like in [20], MIAA (specifically MIAA-t [22]) is the spectral estimation of choice in this article. This is motivated by its simplicity, direct applicability to the nonuniform sampling case, and its good performance for the recovery of point-like targets, which are the main source of artifacts in the low-oversampled staggered SAR case (see remaining of this section for its performance and limitations). In the following, a brief recap of MIAA is provided to aid in the discussion presented in this section. Please refer to [22] for a detailed description of the algorithm.

The complete data segment  $y$  is modeled as

$$y_{N \times 1} = \mathbf{A} \alpha = \begin{bmatrix} e^{j\omega_0 t_0} & & e^{j\omega_{K-1} t_0} \\ \vdots & \ddots & \vdots \\ e^{j\omega_0 t_{N-1}} & & e^{j\omega_{K-1} t_{N-1}} \end{bmatrix} \quad (9)$$

where  $\mathbf{A}_{N \times K}$  is the steering matrix,  $\alpha$  is the spectrum, and  $\omega_k$  are the frequency instants, usually assumed uniformly sampled (i.e.,  $\omega_k = k\Delta\omega$ ), and  $\{t_n\}_0^{N-1}$  are the time instants.

In each iteration  $i$ , the MIAA spectrum is estimated as

$$\hat{\alpha}[\omega_k]_i = \frac{a_g^H[\omega_k] \hat{\mathbf{R}}_{g_{i-1}}^{-1} y_g}{a_g^H[\omega_k] \hat{\mathbf{R}}_{g_{i-1}}^{-1} a_g[\omega_k]} \quad (10)$$

where

$$a_g[\omega_k] = [e^{j\omega_k t_{g,0}} \dots e^{j\omega_k t_{g,G-1}}] \quad (11)$$

with  $\{t_g\}_0^{G-1}$  being the subset of the time vector segment containing only the available instants. The computation of the spectrum in (10) requires the covariance matrix estimated from the data in the previous iteration, with

$$\hat{\mathbf{R}}_{g_i} = \begin{cases} \sum_{k=0}^{K-1} |\hat{\alpha}[\omega_k]|^2 a_g a_g^H, & i \neq 0 \\ \mathbf{I}_G, & i = 0 \end{cases} \quad (12)$$

where  $\mathbf{I}$  is the identity matrix. Once the estimation of the spectrum has converged (e.g., once  $\sum(|\hat{\alpha}[\omega_k]_i - \hat{\alpha}[\omega_k]_{i-1}|^2) < 1e-5$ ), the missing samples are inverted as

$$\hat{y}_m = \sum_{k=0}^{K-1} |\hat{\alpha}[\omega_k]|^2 a_g^H[\omega_k] \hat{\mathbf{R}}_{g_{i-1}}^{-1} y_g a_m[\omega_k] \quad (13)$$

where

$$a_m[\omega_k] = [e^{j\omega_k t_{m,0}} \dots e^{j\omega_k t_{m,M-1}}] \quad (14)$$

with  $\{t_m\}_0^{M-1}$  being the subset of the time vector segment containing missing data instants.

2) *Impact of the Type of Target*: Fig. 4 shows the performance of the blockage reconstruction in terms of the mean oversampling factor for two different type of targets. At the top right, the normalized root mean square error (NRMSE) for an ideal point target after data recovery, resampling and azimuth compression is shown. The NRMSE for simulated distributed scatters appears at the bottom left, and the corresponding coherence degradation is shown at the bottom right.

Different oversampling cases were simulated by varying the mean PRF on transmitter and considering a fixed set of parameters, namely, chirp duration, azimuth bandwidth, swath, and range position. In all cases, we adopted the optimum PRI sequence design described in [5], ensuring that no consecutive azimuth samples are missing in the raw-data domain. For the parameters considered (see second column of Table I), the maximum oversampling ratio that allows for this condition to be met was around 2.1. Two missing samples patterns were considered: one corresponding to the actual blockage in the raw data domain, and the other corresponding to the extended blockage in the range-compressed domain (i.e., imposing full range resolution [25]). The obtained data loss percentage for both cases is shown in Fig. 4, at the top left. The adopted reconstruction

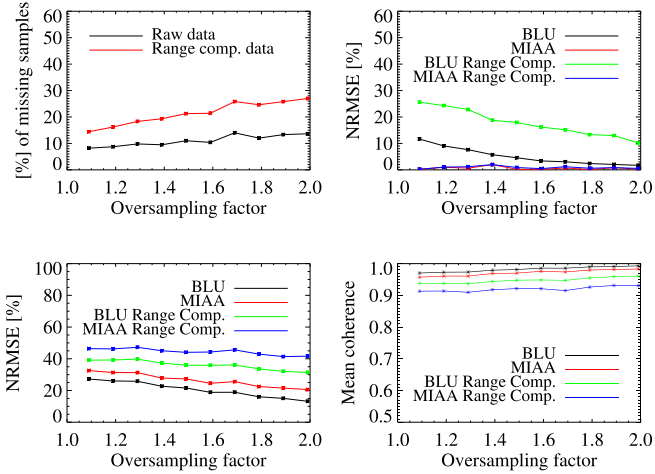


Fig. 4. Performance of the blockage recovery as a function of the oversampling for different recovery methods and processing approaches. (Top left) The percentage of missing samples in the echo. Top right: the NRMSE after reconstruction, resampling and compression for an ideal point target. Bottom left: the NRMSE for distributed scatters. Bottom right: the corresponding coherence between reconstructed data and data with no blockage.

strategy follows the one in [36], where small segments around each missing event (one or more missing samples) are treated separately.

Note that even for oversampling factors of 1.1, the SE yields good results for point targets, regardless of the blockage percentage. On the other hand, the increased amount of missing data in the range compressed case considerably decreases the quality of the BLU reconstruction for the oversampling ratios considered. As the oversampling increases, the reconstruction error with BLU approaches the one with the SE. In fact, for oversampling ratios larger than 1.9 (e.g., as is the case of the standard Tandem-L modes), the use of MIAA does not improve the overall performance in comparison to applying BLU in the raw data domain.

In the case of pure distributed scatters, the reconstruction considering the raw domain blockage is better than the one considering the range-compressed blockage, regardless the recovery method. This is because the auto-correlation of the distributed scatters decays faster in comparison to the one of point-targets, and the recovery is more impacted by the overall increased amount of missing samples (and possibly adjacent blockage) in the range-compressed domain. The coherence degradation caused by applying MIAA to raw data is small in comparison with the one using BLU, specially for larger oversampling ratios. On the other hand, the performance degradation caused by applying MIAA to range-compressed data in comparison to the one of applying BLU in the raw data is significant. For example, for an oversampling ratio of around 1.09 (i.e., experimental Tandem-L case), the coherence goes from around 0.97 using BLU in the raw data domain to 0.9 using MIAA in the range-compressed domain. The performance of all strategies improves with increasing oversampling rates, but at a lower rate for distributed scatters when compared to point-targets.

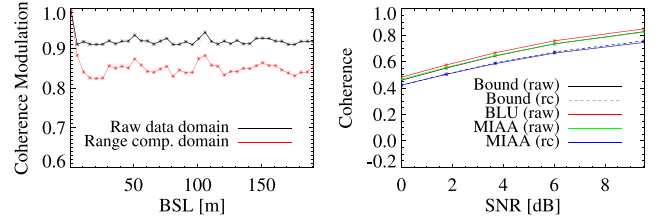


Fig. 5. Left: Decorrelation factor due to staggered operation for varying along-track baseline. Right: estimated coherence from simulated distributed scatters for varying SNR and an along-track baseline of 10 m.

A lower bound for the coherence degradation over distributed scatters can be obtained considering the case where the blockage samples are set to zero. In this case, the azimuth-dependent coherence modulation can be approximated as

$$\gamma_{\text{stag}}[n] = \frac{\sum_{-LSA/2}^{+LSA/2} (\Pi_m G_m) (\Pi_s G_s)}{\sqrt{\sum_{-LSA/2}^{+LSA/2} (\Pi_m G_m)^2 \sum_{-LSA/2}^{+LSA/2} (\Pi_s G_s)^2}} \quad (15)$$

where the terms  $G_*$  include the antenna pattern and the nonuniform (and processing) tapering, and the azimuth dependencies in the right-hand side were omitted for the sake of compactness. This approximation is only meaningful if the signal power is larger than the noise one, and is derived for circular Gaussian processes, i.e., it does not include artifacts (and consequent degradation of the estimated coherence) induced by point targets. In the Tandem-L case, the slave is assumed to be continuously acquired, i.e., it has no blockage and the coherence degradation is independent of the along-track baseline. In the staggered NISAR case, the degradation depends on the relative distribution of the missing samples in master and slave datasets. If the missing samples are perfectly overlapped, no coherence degradation over distributed targets is observed, although a nonnegligible phase bias might be present depending on the amount of blockage within the synthetic aperture [36]. On the other hand, along-track baselines in the order of a few meters are enough to cause the blockage patterns of master and slave to be entirely nonoverlapping, resulting in maximum coherence loss.

The expected coherence modulation as a function of the along-track baseline for the staggered NISAR case is shown in the left of Fig. 5. On the right, the obtained coherence values for different levels of signal-to-noise ratio (SNR) and different interpolation methods are shown for an along track baseline of 10 m. When using MIAA, the obtained coherences are very close to the bounds, i.e., the recovery does not improve the data quality. Note that the actual decorrelation depends on the spectral power of the interpolation error, and is itself a function of the SNR, since a lower SNR results in larger errors.

3) *Impact of SCR*: The point-target simulation results in Fig. 4 consider the reconstruction of a pure point-target, i.e., no noise nor clutter are present. In this case, the reconstruction in the raw-data domain has better performance than in the range-compressed domain, where the amount of missing data due to blockage is larger. However, in real images, strong

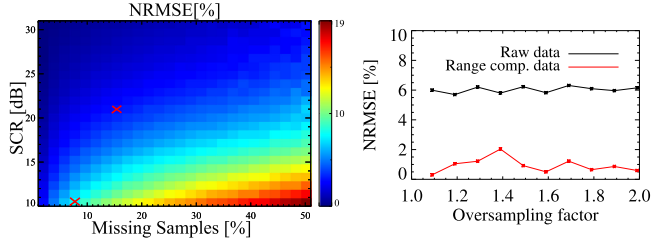


Fig. 6. NRMSE after reconstruction, resampling, and compression for a point target under noise. (Left) Performance for increasing amount of randomly missed samples and SCR. (Right) Performance for the Tandem-L experimental scenario (see Table I) for varying mean PRF on transmitter and a reference SNR value of 15 dB.

targets appear superimposed to noise and clutter. In this case, the signal-to-clutter gain obtained through range compression can benefit the reconstruction of point-targets. This can be observed in the simulation results presented in Fig. 6, where the NRMSE after reconstruction, resampling and compression for a point target under noise is shown. The figure on the left shows the performance as a function of the SNR and amount of missing samples. For this particular simulation, the data were randomly missed, i.e., the optimum PRI sequence design of [5] was not employed, since the goal was to evaluate the effect of different amount of missing data for a given acquisition scenario. An oversampling ratio of 1.09 was considered. Note that a combination of higher SNR and higher amount of missing samples can yield better performance than lower missing samples rate and lower SCR (e.g., see the two red crosses on the left plot of Fig. 6). The plot on the right shows a simulation considering the Tandem-L experimental quad-pol/350 km swath mode, allowing for a variable mean PRF on transmit and considering the expected compression gain in the range-compressed domain. The performance as a function of the oversampling factor considering the reconstruction in the raw-data domain is given by the solid black curve, whereas the one in the range-compressed domain appears in solid red. Regardless of the oversampling rate, the recovery in the range-compressed domain provides better results. For DSs no gain is obtained with the range-compression, and the increasing amount of missing data will degrade the reconstruction in this domain (see Figs. 4 and 5)

4) *Range-Compressed Versus Raw Data Design:* The results in the previous section show that the recovery of point targets using high-resolution SEs profits from increased SCR, even if consecutive missing samples occur. In principle, the PRI sequence design could also be constrained to ensure that no consecutive azimuth samples are missed at range-compressed level [5]. However, such design leads to a faster variation of the PRI subsequences and a larger maximum PRI, which might cause performance degradation despite the thinner gaps. In fact, the simulation results in Fig. 7 show that the range-compressed design does not generally improve the reconstruction. The simulation considered the experimental Tandem-L case, allowing for a varying mean PRF on transmit. The presented curves correspond to two PRI sequence designs: in black, ensuring no consecutive azimuth loss in the raw data domain, and in red

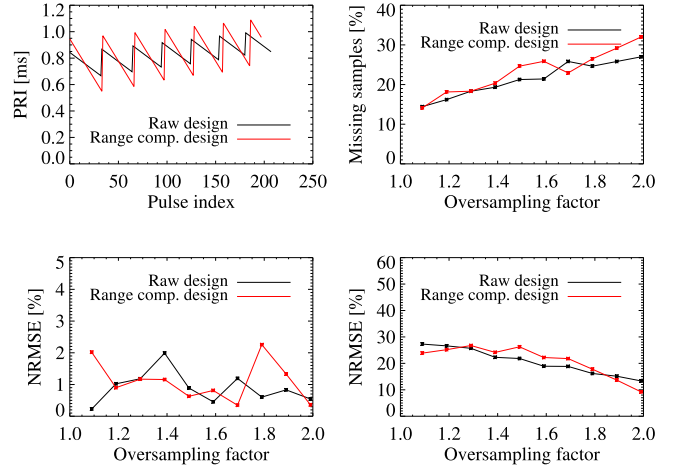


Fig. 7. (Top left) PRI sequences for 10 % oversampling factor. (Top right) The percentage of missing samples. (Bottom left) NRMSE for an ideal point reconstructed in the range-compressed domain with MIAA. (Bottom right) NRMSE for a distributed scatter reconstructed in the raw data domain with BLU. In all plots, the curve in black corresponds to design for no consecutive loss in the raw data domain, while the curve in red corresponds to the design for no consecutive loss in the range-compressed domain.

ensuring no consecutive azimuth loss in the range-compressed domain. The plot on the top left shows the designed PRI sequence (for an oversampling of around 10%); the plot on the top right shows the percentage of missing samples; the plot on the bottom left shows the NRMSE for an ideal point reconstructed in the range-compressed domain with MIAA, and the plot on the bottom right shows the NRMSE for a distributed scatter reconstructed in the raw data domain with BLU. Not only there is no considerable performance gain for point-targets, but also there is a decrease in quality over distributed scatters for several of the considered oversampling factors.

5) *Spectral Grid Characterization:* In the case of nonuniform sampling, the time vector in (9) is given by

$$t_n = (n + r_n) \Delta t \quad (16)$$

where  $\Delta t$  is an approximated constant sampling (e.g., the average sampling of the segment,  $T_m$ ) and  $r_n$  gives the deviation of the sampling instants from the uniform grid. Note that the estimation described in II-B1 makes no assumption regarding time or frequency grids, i.e., it can be directly applied for the recovery of staggered missing data. However, due to the strong nonuniformity of the sampling, the choice of the frequency grid can have a nonnegligible impact on the data recovery.

In [20], the authors define the spectral frequencies as

$$\omega_k = 2\pi k \frac{\Omega_{\max}}{K}, \quad k = 0, K-1 \quad (17)$$

where  $K$  is the total number of spectral samples and the maximum nonambiguous frequency,  $\Omega_{\max}$ , is approximated as the inverse of the mean sampling of the segment, i.e.,  $\Omega_{\max} = \text{PRF}_{\text{mean}}$ . This definition characterizes a spectral support of  $S_{\text{mean}}^+ \subseteq [0, \text{PRF}_{\text{mean}})$ . No discussion on the segment size and spectral sampling (or, conversely  $K$ ) is provided in that



study, except that  $K$  is larger than the number of samples in the segment.

The focusing of complex SAR data acquired at equidistant time intervals considers a spectral support of  $S^\pm \subseteq [-\text{PRF}/2, \text{PRF}/2]$ , where the PRF is greater than the 3 dB Doppler bandwidth,  $B_{\text{az}}$  (we assume here a zero Doppler centroid). In the case of a complete data-set with uniform sampling, the data is usually transformed to the spectral domain using a fast Fourier transform (FFT) with a grid defined by (17) and  $\Omega_{\text{max}} = \text{PRF}$ . In this case, due to the periodicity of the FFT, the obtained spectrum is equivalent to the desired one up to a linear phase term, which is easily accounted for by shifting the azimuth frequency vector during compression. On the other hand, in order to properly model the staggered SAR signal with (9), the negative frequencies have to be explicitly considered. This can be seen by evaluating the elements of the steering matrix  $A$  assuming  $\Delta t = 1/\Omega_{\text{max}}$  in (16), i.e.,

$$A[\omega_{k \pm K/2}, t_n] = e^{j \frac{2\pi}{K} k(n+r_n)} e^{\pm j\pi(n+r_n)}. \quad (18)$$

For the uniform sampling case there are no residuals ( $r_n = 0$ ), and  $A(\omega_{k+K/2}, t_n) = A(\omega_{k-K/2}, t_n)$ , i.e., (9) can be used to describe the desired positive and negative Doppler frequencies (up to a shift). However, this statement is not true for  $0 < |r_n| < 1$ . Hence, in order to properly invert the missing samples, the spectral grid should be defined by

$$\omega_k = 2\pi \left( k - \frac{K}{2} \right) \frac{\Omega_{\text{max}}}{K}, \quad k = 0, K-1 \quad (19)$$

which with  $\Omega_{\text{max}} = \text{PRF}_{\text{mean}}$ , yields the desired support  $S_{\text{mean}}^\pm \subseteq [-\text{PRF}_{\text{mean}}/2, \text{PRF}_{\text{mean}}/2]$ .

As suggested in [21], the spectral sampling can be chosen as a fraction of the resolution of the periodogram, i.e.,

$$\Delta\omega = \frac{1}{(t_n - t_1)p} \quad (20)$$

with  $p$  typically between 5 and 10, and the total number of spectral samples selected as [21]

$$K = \lfloor \text{PRF}_{\text{mean}} / \Delta\omega \rfloor \quad (21)$$

where  $\lfloor \cdot \rfloor$  is the floor operator.

Note that the spectral support does not have to be limited to  $\text{PRF}_{\text{mean}}$ . In fact, it is known that in the case of nonuniform sampling, the maximum nonambiguous frequency which can be recovered can be even larger than  $\text{PRF}_{\text{max}}$  [39]. In [21], the authors suggest the use of the spectral window in order to compute the maximum allowed frequency. In the case of staggered SAR, the window can be calculated considering the valid samples as

$$W[\omega_k] = \left| \sum_{n=0}^{N_g-1} e^{j\omega_k t_{g,n}} \right| \quad (22)$$

and chosen according to the first frequency larger than zero for which  $W(2\pi\Omega_{\text{win}}) \approx 1$ , i.e.,  $S_{\text{win}}^\pm \subseteq [-\Omega_{\text{win}}/2, \Omega_{\text{win}}/2]$ .

Fig. 8 shows the obtained of the NRMSE for a point target after recovery and focusing using different spectral supports for MIAA. The curve in black corresponds to the result obtained

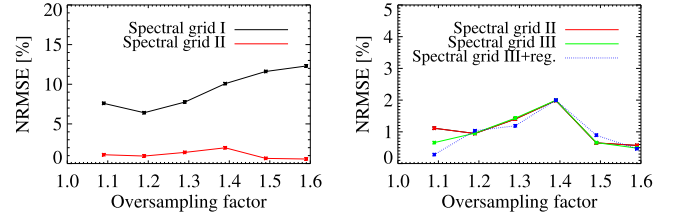


Fig. 8. NRMSE for a point target after reconstruction and focusing considering different spectral grid choices, with and without regularization: The curve in black corresponds to the result obtained with  $S_{\text{mean}}^+$ , the curve in red shows the result obtained with  $S_{\text{mean}}^\pm$  and the curve in green shows the result with  $S_{\text{win}}^\pm$ .

with  $S_{\text{mean}}^+$ , the curve in red shows the result obtained with  $S_{\text{mean}}^\pm$  and the curve in green shows the result with  $S_{\text{win}}^\pm$ . The plots were separated in two for visualization purposes. In all cases, the number of spectral samples was given by (21) and (20) with  $p = 5$ . The blockage for the reconstruction in the range-compressed domain was considered, i.e., double gaps might occur. The quality degradation when using the positive support is evident for all oversampling ratios. It is possible to see that the positive/negative spectral support gives better results. Moreover, as the oversampling increases, the result using (17) degrades. This is due to an increase of the span between maximum and minimum PRIs within the sequence and the consequent worse modeling of the data using (17) and (9). The use of the spectral window, and consequent slightly wider support is only marginally beneficial and only for the case with very low oversampling, where the average PRF is very close to processed Doppler bandwidth.

6) *Model Regularization*: Depending on the nonuniformity pattern and missing data location, the covariance matrix estimated from the available samples can become rank deficient [40], [41]. In fact, this is often the case in the staggered SAR scenario due to the strong variation of the sampling in the segment.

As a regularization alternative, we suggest to directly use the scheme proposed in [41] for IAA, but now considering the missing samples scenario, i.e.,

$$\hat{\mathbf{R}} = \sum_{m \in \xi} |\hat{\alpha}|^2 a_g a_g^H + \sum_{m \in [1, K] \setminus \xi} |\hat{\alpha}|^2 \mathbf{I} \quad (23)$$

where  $\mathbf{I}$  is the identity matrix and  $\xi$  represents the subset of  $[1, K]$  containing the  $N_g$  largest values of the spectral power. As discussed in [41], the justification for (23) is that from a segment with  $N_g$  valid samples we can reliably estimate  $N_g$  spectral components.

The blue curve in Fig. 8 shows the obtained NRMSE when considering the regularization. For the very low oversampling scenario, the regularization brings a small improvement and mitigates sampling-related asymmetry in the recovered IRF.

7) *Choice of Segment Size*: Large kernels can be helpful for the data recovery with conventional algorithms due to noise suppression. However, in the recovery or staggered data with super-resolution SEs, this is not necessarily the case. This is due to the fact that large residuals in (16) often result in pathological



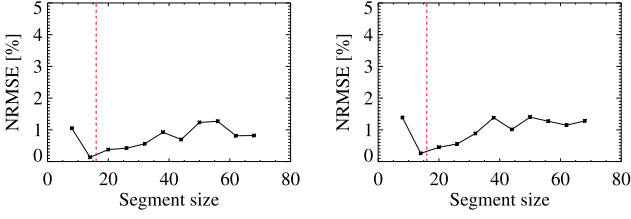


Fig. 9. NRMSE for a point target after reconstruction and focusing considering different segment sizes. The plot on the left corresponds to the raw-data blockage pattern, while the one on the right corresponds to the range-compressed one. The vertical line in red indicates the size obtained with the heuristic described in this section.

samplings, leading to ill-condition covariance matrices. As discussed in the previous section, regularization approaches can be used to prevent quality degradation due to this effect. However, the use of smaller segments can also aid in the inversion. Small segments are also preferred from a computational cost perspective, since algorithms such as MIAA are very demanding due to the operations with large matrices.

Neglecting noise, an heuristic to select the segment size for the data recovery is to evaluate the maximum deviation of the actual sampling to its best uniform sampling approximation. For example, a good segment size would be the largest size for which the maximum deviation to this uniform grid is smaller than half of the uniform sampling step. Fig. 9 shows NRMSE for a point target after reconstruction and focusing considering different segment sizes. The recovery was performed considering the regularization described in the previous section. The plot on the left corresponds to the raw-data blockage pattern, while the one on the right corresponds to the range-compressed one. The vertical lines in red indicate the sizes obtained with the heuristic described above. In both cases, there is a good agreement between the obtained sizes and minimum NRMSE.

### III. MODIFIED TWO-STEP RECONSTRUCTION FOR LOW-OVERSAMPLED STAGGERED SAR DATA

From the performance analysis presented in the previous section, it is clear that the reconstruction of point-targets and DSs have conflicting characteristics: while the former generally benefits from the range-compression, the latter has better performance if carried out in the raw-data domain. Moreover, super-resolution SEs have a positive impact for point-like targets only, although its performance degradation over distributed scatters can be acceptable considering the recovery at raw data domain, depending on performance requirements and system characteristics (e.g., oversampling rate and chirp duration).

In order to accommodate these somewhat conflicting requirements, we propose a modified strategy for the handling of low-oversampled staggered data. As in [20], blockage recovery and resampling to the uniform grid (when necessary) are performed in independent steps. However, our strategy contains the following particularities.

- 1) The recovery of the blockage is performed twice: first, at raw data level and then at range-compressed level. While the second recovery step employs a high-resolution SE

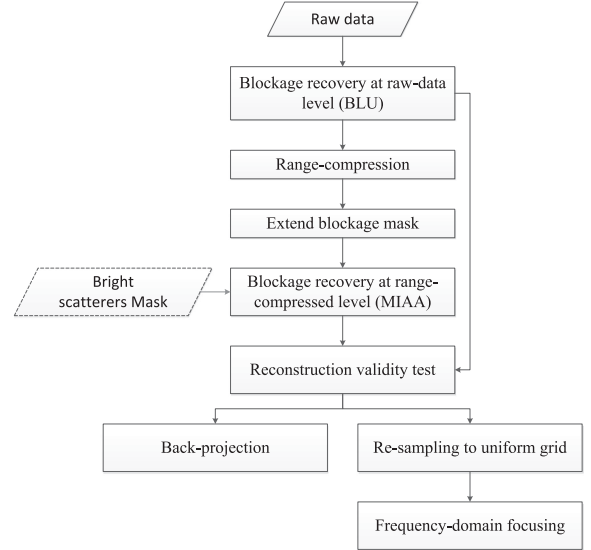


Fig. 10. Block diagram preprocessing strategy for low-oversampled staggered SAR data.

and focus on the recovery of point-like targets, the first one is performed with BLU.

- 2) A validity test is performed in order to accept or not the result of the SE in order to avoid degradation over distributed scatters.
- 3) The spectral-estimation based recovery is applied over small segments rather than over the complete synthetic aperture.

Our proposed approach for the handling of low-oversampled staggered data is summarized in the block diagram shown in Fig. 10. In the following, the processing steps are discussed.

8) *Blockage Recovery at Raw-Data Level:* As discussed in II-A, even if considering a back-projection kernel for the focusing, the recovery of the missing data from the blocked instants is required for the low-oversampling staggered SAR scenario. Accordingly, the first step of the proposed approach is the recovery of all the blockage at raw-data level. As indicated in Fig. 10, the result of this first recovery is later used to aid in the validation of the high-resolution spectral-estimation. We suggest the use of the BLU interpolator for this step, since it has optimum performance for distributed scatters and can be implemented efficiently considering the periodicity of the PRI variation [5]. Moreover, it is known to have a better performance in terms of noise scaling when compared to multichannel strategies, as the one used in [20].

9) *Extension of Blockage Matrix:* Since the reconstruction of strong targets is performed in the range-compressed domain, the missing data matrix (binary matrix indicating the positions of the blockage) has to be dilated in range in order to account for partially available echoes, which are treated here as invalid, i.e.,

$$M_{\text{block}_{\text{RC}}} = M_{\text{block}_{\text{raw}}} \oplus S \quad (24)$$

where  $M_{\text{block}_{\text{raw}}}$  and  $M_{\text{block}_{\text{RC}}}$  are the missing data matrices in the raw-data and range-compressed domains, respectively, and assume 1 for missing data and 0 otherwise.  $S$  is the 1-D

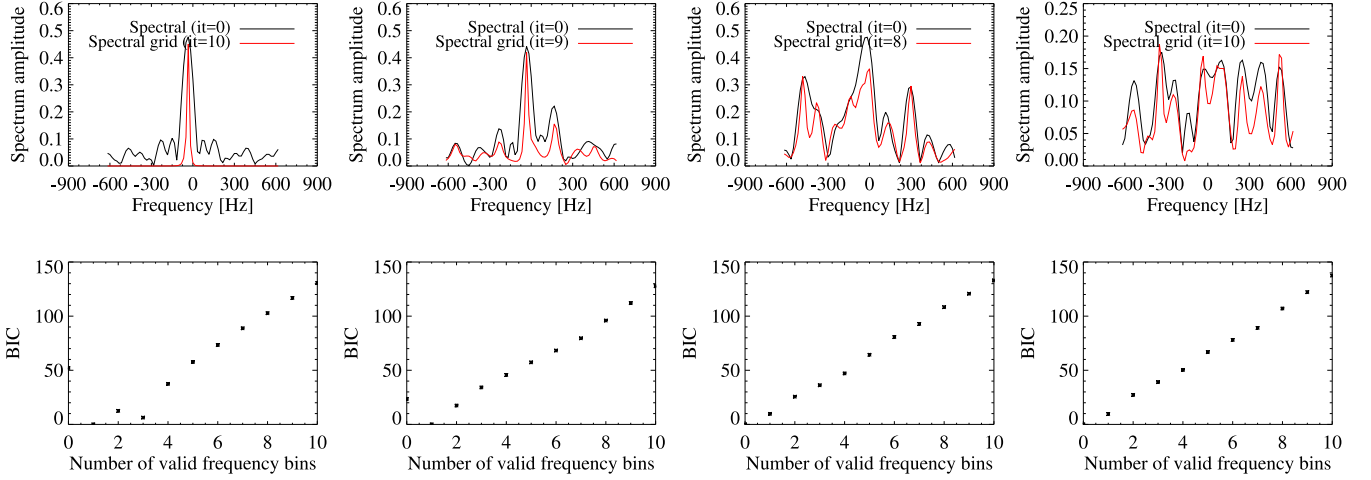


Fig. 11. (Top) Spectrum estimated with MIAA at its first iteration (in black), and upon convergence (in red). (Bottom) The BIC criteria as a function of spectral components. From left to right: Pure point-target, Point target plus noise (SNR=12 dB), Point target plus noise (SNR=3 dB) and clutter.

structuring element given by

$$S = [1 \cdots 1]_{1 \times N_{\text{chirp}}} \quad (25)$$

where  $N_{\text{chirp}}$  is the chirp length in samples. As discussed in Section II-B, although the recovery step is performed on the range-compressed data, the PRI sequence is still designed considering the reconstruction in the raw-data domain, i.e.,  $M_{\text{block}_{\text{RC}}}$  might indicate consecutive missing samples in azimuth.

**10) Blockage Recovery at Range-Compressed-Data Level:** After the range compression and the retrieval of the extended blockage mask, the second recovery step is performed by means of a high resolution SE (in this study, MIAA). As mentioned in II-B, we perform the estimation for each range bin separately, and the 1-D signal is divided into small segments whose size are determined using the heuristic described in Section II-B7 (typically between 12-20 samples). The computation of the spectrum follows on the grid defined by (19)–(21), with  $p = 5$ . The estimation of the covariance matrix within MIAA is performed with (23) in order to minimize the reconstruction error over point-like targets and avoid asymmetries in recovered IRFs.

Note that the block-diagram includes the optional use of a “Bright scatterers mask” (dashed box). The main purpose of this mask is to diminish the overall computational burden by avoiding the second recovery step over segments with very low back-scatter. Note that, for these kind of targets, the result based on spectral estimation techniques is likely to be invalid. Assuming that bright targets do not dominate the scene content, this mask can be created by applying a simple outlier detector in the amplitude after range-compression. The mask is then dilated in both range and azimuth directions in order to diminish miss-detection and to “close” dark areas corresponding to the data poorly interpolated with BLU.

**11) Validity Test:** From the characteristics of the spectrum estimated in the previous step, we can attempt to distinguish valid from invalid recoveries. This can be accomplished, e.g.,

by using the Bayesian information criterion (BIC). The BIC rule is defined as [21]

$$\text{BIC}[M] = N \ln \left( \sum_{n=1}^N \left| y[t_n] - \sum_{k=1}^M \hat{\alpha}_{\text{ordered}}[\omega_k] e^{j\omega_k \text{ordered } t_n} \right|^2 \right) + 4M \ln N \quad (26)$$

where the first term is a least-square data fitting term, which gives the error of the data if reconstructed by the  $M$  largest estimated spectral components, and the second term penalizes the complexity of the estimated spectrum. If  $\text{BIC}(0)$  is the minimum BIC, the data consist of white noise and the estimation using MIAA is considered invalid. Fig. 11 shows an example of the estimated spectrum of a certain segment containing missing data. The plots correspond to simulated data considering the Tandem-L experimental quad-pol mode. The plots on the top row show the spectrum estimated with MIAA in its first iteration (in black), and upon convergence (in red). The plots at the bottom show the BIC criteria as a function of valid spectral components. Four cases are considered, from left to right: Pure point-target, Point target plus noise (SNR=12 dB), Point target plus noise (SNR=3 dB) and clutter. Note that for the last two cases, the BIC criteria deems the estimation with MIAA invalid. In fact, although BIC is able to correctly detect valid recoveries from strong point targets, the criteria suffers with misdetection of segments containing weaker point targets specially toward the end of the synthetic aperture. Hence, we propose a validation cross-check step employing the initial recovery at raw data level.

Specifically, we consider the recovery based on spectral estimation techniques of a segment to be invalid if the following conditions are met

$$\arg \min_M \text{BIC}[M] = 0 \quad (27)$$

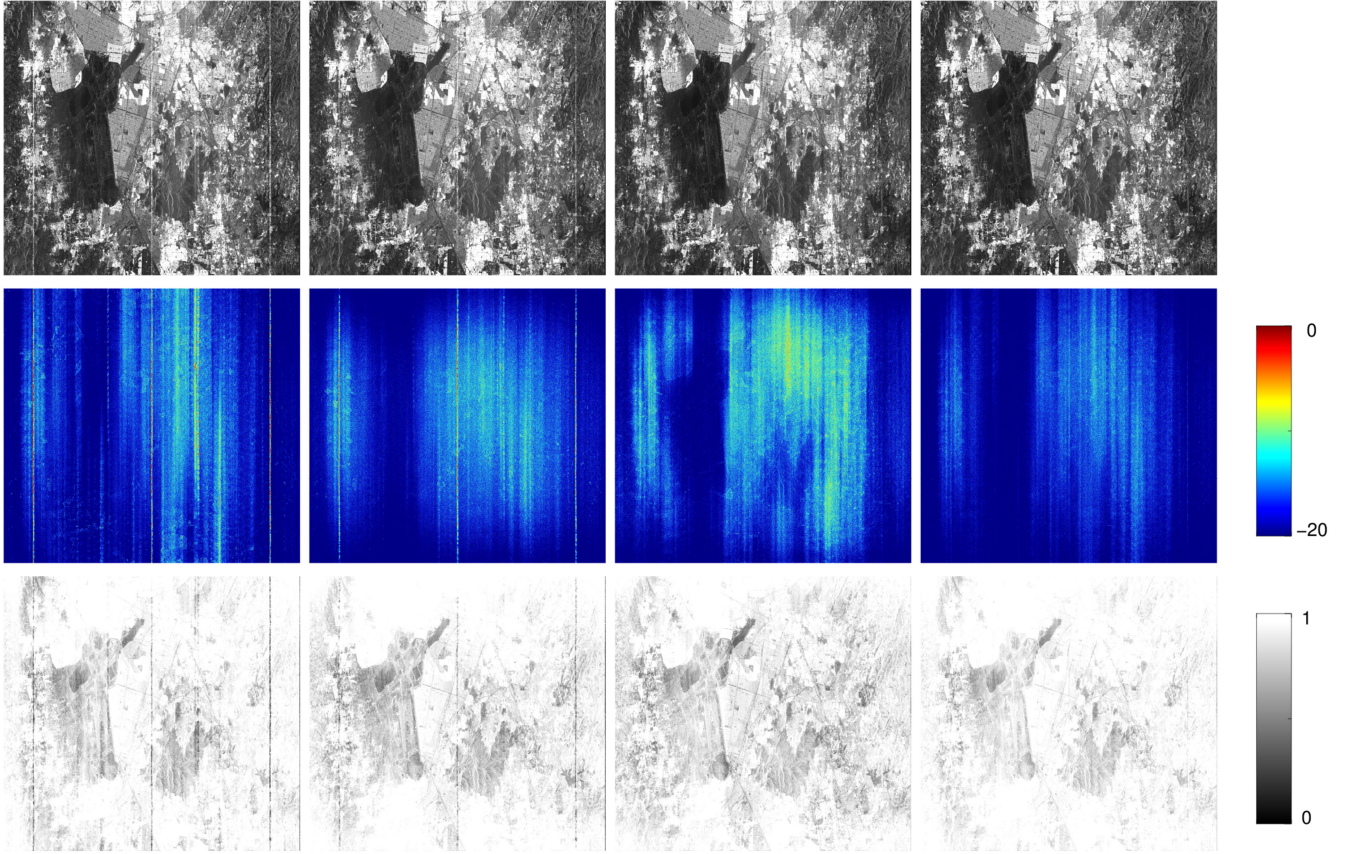


Fig. 12. (Top) Amplitude, (middle) difference in dB between recovered data and non-blocked reference, and (bottom) coherence with respect to reference. The following blockage interpolation methods were used, from left to right: BLU, MIAA in the raw-data domain (equivalent to the blockage recovery in [20]), MIAA in the range-compressed domain, and the proposed approach.

and

$$\begin{aligned}
 & \frac{1}{N-1} \sum_{n=1}^N |y_{\text{RAWest}}[t_n] - \bar{y}_{\text{RAWest}}|^2 \\
 & \geq \frac{1}{N-1} \sum_{n=1}^N |y_{\text{RCest}}[t_n] - \bar{y}_{\text{RCest}}|^2 \quad (28)
 \end{aligned}$$

i.e., if the estimated spectrum is considered too complex and the resulting segment is less smooth than the one filled with data originating from the raw-data domain recovery.

As a final remark, note that, as is the case in [20], the quality of the recovered data using the strategy proposed here is bounded to that of staggered data acquired with no blockage, i.e., artifacts related to the nonlimitation of the azimuth spectrum and to the nonuniformity or eventual under-sampling of the nonblocked sampling pattern will still be present.

#### IV. RESULTS WITH SIMULATED STAGGERED SAR DATA

In this section, we present results obtained with synthetic data from the DLR-HR end-to-end simulator [42], [43]. The simulator used an input L-band reflectivity map retrieved from an ALOS-2 acquisition over Mexico City, and was used to generate data emulating both the Tandem-L experimental mode

(parameters in the second column of Table I) and the NISAR staggered scenario (parameters in the third column of Table I).

##### A. NISAR Staggered Scenario

Fig. 12 shows the results obtained for the NISAR staggered scenario using different blockage recovery strategies. The recovery methods were, from left to right: BLU, MIAA in the raw-data domain (equivalent to the blockage recovery proposed in [20]), MIAA in the range-compressed domain, and the proposed hybrid approach. The plots on the top row show the normalized amplitude images, the plots in the middle show the difference in dB between the recovered images and the reference (i.e., the staggered SAR image with no blockage), and the images in the bottom row show the coherence between the recovered images and the nonblocked reference. In this simulation, three additional point-targets with a SCR above 50 dB were introduced at near-, middle-, and far-range, and they are clearly visible in the images, where the reconstruction occurs at raw-data level (see red lines along azimuth in the difference plots in the first and second columns). When recovering with MIAA in the range-compressed domain (third column), the artefacts of strong targets are suppressed at the expense of overall coherence reduction. Finally, the proposed two-steps recovery is able to suppress the strongest artefacts, while maintaining



TABLE II  
COMPUTATION TIME OF THE RECOVERY METHODS USED FOR THE  
RESULTS SHOWN IN FIG. 12

Method	Data recovery time
BLU	1 min
MIAA in the raw-data domain	200 min
MIAA in the range-compressed domain	170 min
Proposed hybrid approach	171 min

the decorrelation to the same level obtained with BLU. The computation times of the four methods used for the data recovery of the results shown in Fig. 12 are given in Table II. The computations were performed on an Intel(R) Xeon(R) CPU X7560 @ 2.27 GHz machine with 32 CPUs and 398 GB of RAM. Each method was limited to 12 parallel threads, and the complete data matrix had  $11\text{ k} \times 11\text{ k}$  samples. In this particular example, although the amount of missing samples is larger in the range-compressed domain (around 15% of the data amount, against 8% in the raw-data domain), the computation time of the third and fourth approaches are smaller than the one of the second approach. This is because MIAA tends to converge faster for targets with increased SCR, i.e., it is potentially faster in the range-compressed domain. Finally, note that the implementation of MIAA was not optimized and the computation time of the hybrid approach can be reduced by using a mask to detect strong targets, as mentioned in Section III-10.

In order to evaluate the impact on interferometry, the DLR-HR end-to-end simulator was used to generate a stack with 20 images and along-track baselines uniformly distributed in the interval between  $\pm 110\text{ m}$ . A series of 50 almost aligned strong point-targets were included in the image (signal-to-clutter ratio larger than 50 dB). The distribution of the targets and their power in this rare scenario can severely impact the staggered SAR performance. Two areas of linear deformation were simulated, as well as atmospheric disturbances. Examples of the residual interferometric phases (i.e., without the topographic phase, the deformation and the atmospheric phase screen) are shown in Fig. 13. The results with BLU are shown on the top row, and the results with the proposed approach on the bottom row. Strong artifacts associated with the point-targets are clearly recognized, and their behavior varies according to the baseline. The artifacts are mainly reduced using the spectral estimation approach, although residual noise is still visible. Fig. 14 shows the obtained residual phase histograms when using BLU (solid black) and the proposed approach (solid red). The histograms were computed considering the central third of the image, i.e., only the area most affected by the artefacts, and show a residual standard deviation of around  $10^\circ$  when using the proposed approach.

Persistent scatterers (PSs) were detected at full resolution considering an amplitude dispersion threshold of 0.2. The PSs were then processed and the mean differential deformation velocity was estimated. Arcs with a model coherence greater than 0.85 were considered valid and, after integration, a verification was performed to detect inconsistencies in the integrated mean deformation velocity. The estimated mean velocities are shown in Fig. 15 (BLU on the left, MIAA in the middle). The difference between the mean velocity maps appears on the right

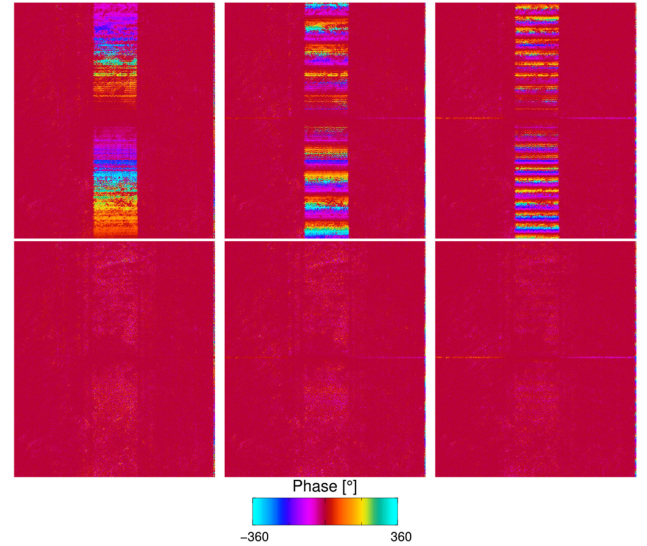


Fig. 13. Residual interferometric phases for along-track baselines of (left) 10 m, (middle) 50 m and (right) 110 m. Results with (top row) BLU and (bottom row) with the proposed approach.

(for the common points). It is possible to see that despite the strong targets, the mean deformation velocity is mainly well estimated in both cases. This is because most side-lobes do not overlap in the different slaves and the effects cancel in average. Nevertheless, the BLU map contains a few residual biases (see red ovals). The larger the baseline diversity, the less likely such biases will be. In both estimations, it is possible to see that (residual) artifacts reduced the number of valid points detected in the middle stripe where the strong-point targets dominate. This effect will be reduced if temporal coherence instead of amplitude dispersion (and DSs instead of PSs) are used. Finally, note that both maps contain residual noise mainly due to the staggered operation. To quantify the noise, a stack without any deformation or atmosphere was simulated. The resulting standard deviation of the estimated mean deformation velocity was around 0.045 cm/month for BLU and 0.048 cm/month for the spectral estimation approach. For the same configuration, the standard deviation obtained using a reference stack formed by images with a constant PRF was around 0.02 cm/month.

#### B. Tandem-L Experimental Quad-Pol Scenario

The bandwidth of the transmitted signal in the Tandem-L quad-pol experimental scenario is larger than the NISAR one, which results in the strong artefacts being more smeared after range-cell migration correction [44]. Nevertheless, SEs can still improve the recovery of point-like targets as suggested by the performance analysis in Section II-B.

Unlike NISAR, Tandem-L is envisioned as a single-pass bistatic interferometer, and the decorrelation caused by the low-oversampled staggered operation will be more visible in the single-pass interferograms. A cross-platform approach to recover the blockage in the Tandem-L quad-pol experimental scenario—similar to what we proposed in [36] for the retrieval of the missing caused by the synchronization link in TanDEM-X

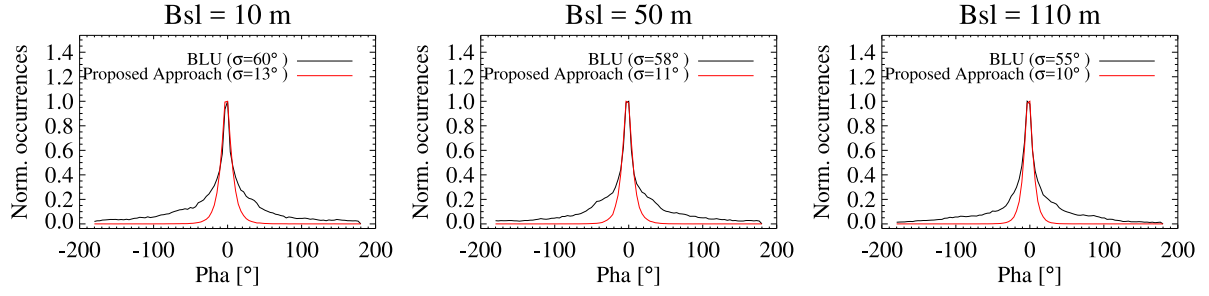


Fig. 14. Phase histograms over a region of interest containing the strongest artefacts at the center of the scene. The plot in the left corresponds to the 10 m baseline case, in the middle to the 50 m baseline case, and on the right to the 110 m baseline case. The curves in black show the results using BLU, whereas the one in red show the results with the proposed approach.

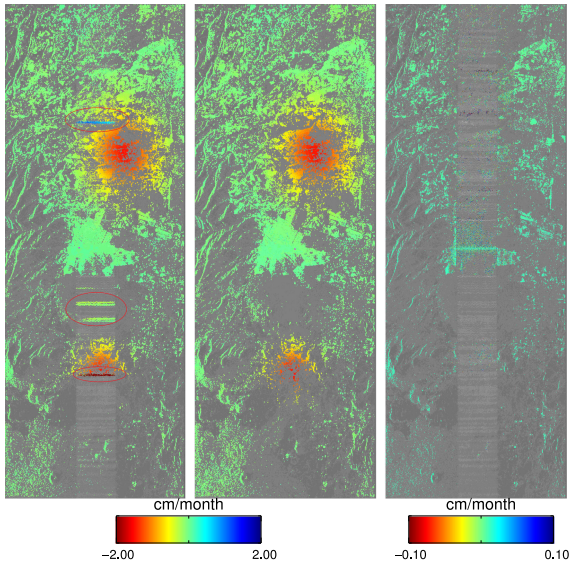


Fig. 15. Estimated mean deformation velocity with (left) BLU and (middle) the proposed approach. The difference map for common PSs appears on the right over the reflectivity image obtained with BLU.

data—could be an option to maximize the bistatic coherence while minimizing phase noise and/or artefacts. Since the current plan for Tandem-L is to have continuous acquisition by the slave system (i.e., the slave image would have no missing data), the bistatic data could be always used to interpolate the monostatic one, regardless of the along-track baseline (naturally, with varying performance according to the spectral overlap). The cross-platform interpolation requires the compensation of the response of one system with respect to the other, e.g., compensation for different system gains or antenna patterns, among others. However, the effects of the lack of precise calibration information and of changes in the back-scatter of semitransparent media due to the different geometries have to be further investigated.

A suboptimal approach which can decrease the decorrelation caused by the staggered operation is to match the processing filters. Specifically, blockage can be forced on the originally nonblocked coregistered bistatic slave at the same positions where the blockage of the monostatic master is expected to be. This will degrade the quality of the bistatic image, but can reduce coherence loss. An example considering such strategy is

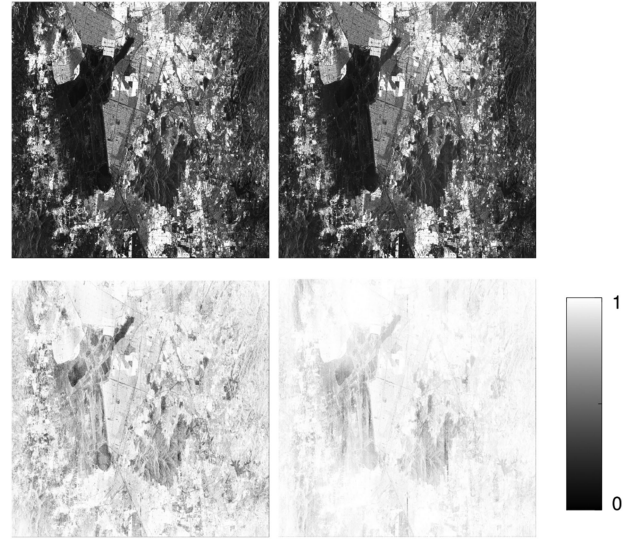


Fig. 16. (Top) Bistatic slave amplitude and (bottom) single-pass interferometric coherence, for an along-track baseline of 100 m and zero across-track baseline. For the results on the left column, the proposed approach was employed to correct the blockage of the master and the slave has no blockage. For the results on the right column, the master blockage was forced on the slave and the proposed approach was applied to both images.

shown in Fig. 16. The figures on the top show the bistatic slave amplitudes, and the ones on the bottom show the single-pass interferometric coherences. An along-track baseline of 100 m and zero across-track baseline were considered. For the results on the left column, the proposed approach was employed to correct the blockage of the master while the slave has no blockage. For the results on the right column, the master blockage was forced on the slave raw data and the proposed approach was applied to both acquisitions. Although such approach can improve the performance of coherence based applications, it can also lead to phase biases depending on the blockage distribution within the synthetic aperture and on the quality of the interpolation. Moreover, it is clearly not indicated for amplitude-based applications, due to the inherent decreased quality loss of the slave image. As stated earlier, better performance can be potentially obtained if we interpolate the master blockage using information from the bistatic slave. This is the topic of a follow-on research work.



## V. CONCLUSION

In this article, we proposed an alternative strategy for the handling of low-oversampled staggered SAR data. The approach relies on the recovery of the blockage data using spectral-estimation techniques applied to data in the range-compressed domain, and on the discrimination between valid and invalid recovery results based on the characteristics of the estimated spectra. We validated the methodology with simulations considering the experimental Tandem-L fully polarimetric 350 km swath mode, and an eventual staggered NISAR scenario with chirp duration of 47  $\mu$ s and swath of 240 km. The obtained results confirm that the proposed approach is a viable solution for future systems and/or modes which cannot afford the high oversampling ratio required for standard staggered SAR operation.

Although the proposed approach relies on the use of BLU and MIAA as the interpolators in the raw-data domain and range-compressed domain, those can be replaced by other interpolators according to availability. For example, the use of SEs, which consider a certain spectral extent [45] or newly developed SEs for mixed spectra [46] could be evaluated as an alternative to MIAA, at the possible expense of computational complexity.

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